

ChE/MSE 505  
Advanced Mathematic for Engineers  
Final Exam  
Fall Semester, 2006  
Instructor: David Keffer  
Administered: 8:00-10:00 am, Monday December 11, 2004

**Problem 1.**

We want to use the following equation to fit some vapor pressure data.

$$P^{vap} = \exp\left(\frac{A}{B+T}\right) \quad (4)$$

where  $T$  is temperature and  $A$  and  $B$  are fitting constants. We have two pieces of data: the vapor pressure at 600 K is 8 atm and the vapor pressure at 620 K is 10 atm. Given this experimental data find the best values of  $A$  and  $B$ .

**Problem 2.** Consider the integral equation

$$\phi(x) = f(x) + \lambda \left[ \int_{x_0}^x N(x, y)\phi(y)dy \right]$$

where

$$f(x) = x$$

$$N(x, y) = x(y+1)$$

$$\lambda = 1$$

$$x_0 = 2$$

- (a) Is this integral equation linear or nonlinear?
- (b) Is this integral equation Volterra or Fredholm?
- (c) Is this integral equation of the first or second kind?
- (d) Use a numerical method to find an approximate solution to  $\phi(x)$  from  $x_0$  to  $x_f=4$ . Use a discretization step of  $\Delta x = 1$ . You are free to solve this as you choose, as long as you state your assumptions. However, I suggest you use the trapezoidal rule to approximate the integral, although that is not mandatory. I would like to see numerical values for the solution. There is no use for calculators in this problem.