

Review Handout for Discrete PDFs

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| <p>A.1. Discrete uniform $f(x;k) = \frac{1}{k}$</p> | <p>k = number of elements in sample space x = outcome is one distinct element</p> |
| <p>A.2. Binomial $b(x;n,p) = \binom{n}{x} p^x q^{n-x}$ Cumulative binomial in Table A.1 of WMM.</p> | <p>n = # of (independent, repeated, with replacement, only 2 outcomes) Bernoulli trials p = probability of success on one trial q = 1 - p = probability of failure on one trial x = # of successes</p> |
| <p>A.3. Multinomial $m(\{x\};n,\{p\},k) = \binom{n}{x_1, x_2, \dots, x_k} \prod_{i=1}^k p_i^{x_i}$</p> | <p>k = # of different types of outcomes n = # of (independent, repeated, with replacement) Bernoulli trials p_i = probability of type i success on one trial x_i = # of successes of type i</p> |
| <p>A.4. Hypergeometric $h(x;N,n,k) = \frac{\binom{k}{x} \binom{N-k}{n-x}}{\binom{N}{n}}$ for x = 0, 1, 2...n</p> | <p>N = # of elements in population n = # of elements in sample, drawn without replacement k = # of outcomes labeled success in population x = # of successes in sample</p> |
| <p>A.5. Multivariate Hypergeometric $h_m(\{x\};N,n,\{a\},k) = \frac{\binom{a_1}{x_1} \binom{a_2}{x_2} \binom{a_3}{x_3} \dots \binom{a_k}{x_k}}{\binom{N}{n}}$</p> | <p>k = # of different types of outcomes N = # of elements in population n = # of elements in sample, drawn without replacement a_i = # of outcomes labeled success of type i in population x_i = # of successes of type i in sample</p> |
| <p>A.6. Negative Binomial $b^*(x;k,p) = \binom{x-1}{k-1} p^k q^{x-k}$ for x = k, k + 1, k + 2...</p> | <p>x = # of (independent, repeated, with replacement, only 2 outcomes) Bernoulli trials p = probability of success on one trial q = 1 - p = probability of failure on one trial k = # of successes</p> |
| <p>A.7. Geometric $g(x;p) = pq^{x-1}$ for x = 1, 2, 3...</p> | <p>x = # of (independent, repeated, with replacement, only 2 outcomes) Bernoulli trials p = probability of success on one trial q = 1 - p = probability of failure on one trial</p> |
| <p>A.8. Poisson $p(x;\lambda t) = \frac{e^{-\lambda t} (\lambda t)^x}{x!}$ for x = 0, 1, 2...</p> | <p>t = the size of the interval λ = the rate of the occurrence of the outcome x = the number of outcomes occurring in interval t. Cumulative Poisson PDF in WMM Table A.2.</p> |

Review Handout for Continuous PDFs

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| <p>B.1. Continuous uniform</p> $f(x; A, B) = \begin{cases} \frac{1}{B - A} & \text{for } A \leq x \leq B \\ 0 & \text{otherwise} \end{cases}$ | <p>A = lower limit of random variable B = upper limit of random variable x = outcome of uniform selection</p> |
| <p>B.2. Normal</p> $f(x; \mu, \sigma) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}$ <p>Cumulative standard normal PDF given in Table A.3 of WMM, need $z = \frac{x-\mu}{\sigma}$</p> | <p>μ = population mean σ = population standard deviation x = random variable of normal PDF</p> |
| <p>B.3. Gamma</p> $f_{\Gamma}(x; \alpha, \beta) = \begin{cases} \frac{1}{\beta^{\alpha}\Gamma(\alpha)} x^{\alpha-1} e^{-x/\beta} & \text{for } x > 0 \\ 0 & \text{elsewhere} \end{cases}$ | <p>α = # of events β = mean time to failure, or mean time between events (must have same units as x) x = time of interest Incomplete Gamma Function given in Table A.24 of WMM, need $y = \frac{x}{\beta}$</p> |
| <p>B.4. Exponential (gamma with $\alpha = 1$)</p> $f_e(x; \beta) = \begin{cases} \frac{1}{\beta} e^{-x/\beta} & \text{for } x > 0 \\ 0 & \text{elsewhere} \end{cases}$ | <p>β = mean time to failure, or mean time between events (must have same units as x) x = time of interest</p> |
| <p>B.5. Chi-squared</p> $f_{\chi^2}(x; \nu)$ <p>Critical values of the Chi-squared distribution are given in Table A.5 of WMM.</p> | <p>$\nu = n-1$ = degrees of freedom, x = random variable $\alpha = 1 - F_{\chi^2}(x; \nu) = P(X > x)$</p> |
| <p>B.6. t-distribution</p> $f_t(x; \nu)$ <p>Critical values of the t-distribution are given in Table A.4 of WMM.</p> | <p>$\nu = n-1$ = degrees of freedom, x = random variable $\alpha = 1 - F_t(x; \nu) = P(X > x)$</p> |
| <p>B.7. F-distribution</p> $f_F(\nu_1, \nu_2)$ <p>Critical values of the F-distribution are given in Table A.6 of WMM.</p> | <p>$\nu_1 = n_1 - 1$ = degrees of freedom of variable 1 $\nu_2 = n_2 - 1$ = degrees of freedom of variable 2 $\alpha = 1 - F_F(x; \nu) = P(X > x)$</p> |